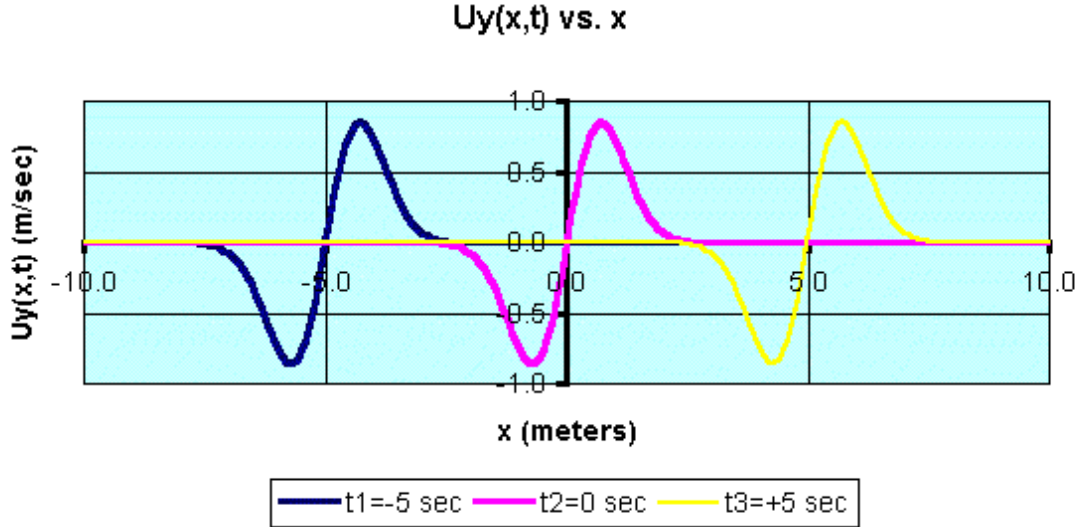


For the right-moving gaussian transverse wave,  $y(x, t) = y_0 \exp\{-(x - v_x t)^2\}$ , with amplitude,  $y_0 = 1.0 \text{ m}$ , and *longitudinal* wave velocity,  $v_x = +1.0 \text{ m/sec}$  the following plot shows the transverse velocity of this wave,  $u_y(x, t) = -(\partial y(x, t)/\partial x) v_x$  as a function of the position,  $x$  on the string, for  $t = -5, 0$  and  $+5$  seconds. Reproducing this plot is left as an exercise for the interested reader - see exercise(s) at the end of these lecture notes.



### Harmonic Traveling Waves

Having discussed the general properties of traveling waves, we now focus specifically on *harmonic* traveling waves - i.e. waves that repeat themselves periodically in space and in time. Harmonic traveling waves are sinusoids - and can be described either by sine or cosine functions - e.g. right-moving harmonic traveling waves can be mathematically described as:

$$y(x, t) = A \sin \left[ 2\pi \left( \frac{x}{\lambda} - \frac{t}{\tau} \right) \right] = A \sin (kx - \omega t)$$

or:

$$y(x, t) = A \cos \left[ 2\pi \left( \frac{x}{\lambda} - \frac{t}{\tau} \right) \right] = A \cos (kx - \omega t)$$

where the *amplitude*,  $A$  (= transverse displacement from equilibrium position,  $y = 0$ ) has units of length (e.g. *meters*), the *wavelength*,  $\lambda$  (in *meters*) which is the spatial repeat distance of a harmonic traveling wave; the *period*,  $\tau$  (units of time, e.g. *seconds*) is the repeat time of the harmonic traveling wave. Related quantities are the *frequency*,  $f = 1/\tau$  (units of *cycles per second*, or *Hertz*), the *angular frequency*,  $\omega = 2\pi f$  (units of *radians/second*, often abbreviated as *rad/sec*), and the *wavenumber*,  $k = 2\pi/\lambda$  (units of inverse length, e.g. *inverse meters* =  $1/\text{m} = \text{m}^{-1}$ ) of the harmonic traveling wave. The longitudinal wave *speed*,  $|v_x|$  (= the *magnitude* of the longitudinal velocity,  $v_x$ ) is related to the frequency and wavelength of the harmonic traveling wave by the relation  $|v_x| = f\lambda$ . Since  $\omega = 2\pi f$  and  $k = 2\pi/\lambda$ , we also have  $|v_x| = (2\pi f)(\lambda/2\pi) = \omega/k$ .