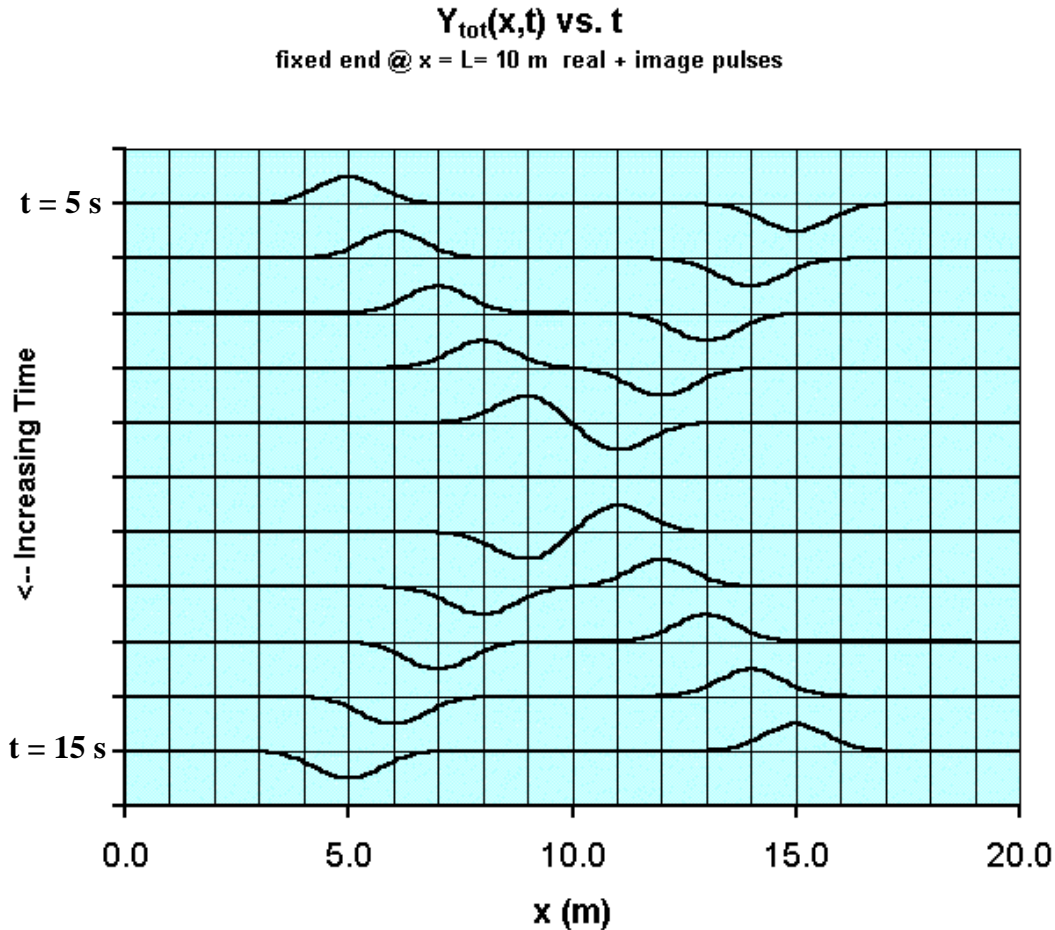


superposed with a polarity-inverted, left-moving transverse traveling wave, which is a “mirror” image of the original wave.

The following plot shows a snapshot time sequence of a right-moving gaussian-shaped transverse traveling wave reflecting from a fixed end, located at  $x = L = 10 \text{ m}$ . The amplitude of the pulse is  $y_0 = 0.5 \text{ m}$ , the longitudinal wave speed  $v_x = 1.0 \text{ m/sec}$ . Note that the sequence of (11) time snapshots progress vertically downward in 1 second steps, starting at  $t = 5 \text{ sec}$ , and ending at  $t = 15 \text{ sec}$ . The left-moving image pulse is used to represent the reflection in the physical region ( $x \leq L = 10 \text{ m}$ ). Note, for the purposes of comparison with free-end reflection (see below), that the slope,  $\partial y_{\text{tot}}(x=L,t)/\partial x$  is not zero at the fixed end, located at  $x = L = 10 \text{ m}$ .



### B.) Reflection of Waves at a Free End

If the end of a taught string, again at  $x = L$  is held fixed *longitudinally*, but is freely able to vibrate *transversely*, for example, by attaching a horizontal string to the end support via a massless, frictionless ring, which can slide transversely (*e.g.* up and down) on a rigid, frictionless rod, the free-end *boundary condition* can be stated mathematically as the requirement that the *slope*,  $\partial y/\partial x$  of the transverse displacement *at the point*  $x = L$  for *any time*  $t$  *must* be zero, *i.e.*  $\partial y(x=L,t)/\partial x = 0$ . Operationally, we first *compute* the