

The sinc function  $\text{sinc}\left[\frac{1}{2}(\omega - \omega_0)\Delta t_0\right] \equiv \frac{\sin\left[\frac{1}{2}(\omega - \omega_0)\Delta t_0\right]}{\left[\frac{1}{2}(\omega - \omega_0)\Delta t_0\right]}$  for sine-wave signals of {short} time duration  $\Delta t_0 = 1\tau_0, 2\tau_0, 3\tau_0, 4\tau_0$  where  $\tau_0 = 1/f_0$  and the corresponding # of cycles of oscillation  $N_c \equiv \Delta t_0/\tau_0 = 1, 2, 3, 4$  are shown in the figure below. Note that the **width**  $\Delta f_0$  of the main peak (at  $f = f_0$ ) depends **inversely** on the time duration  $\Delta t_0$  of the signal, due to the **uncertainty principle**  $\Delta f \Delta t = 1$ .

