

Sound Intensity Level:

The human ear responds ~ *logarithmically* to sound intensity:

Loudness = Sound Intensity Level, $L_I = SIL$:

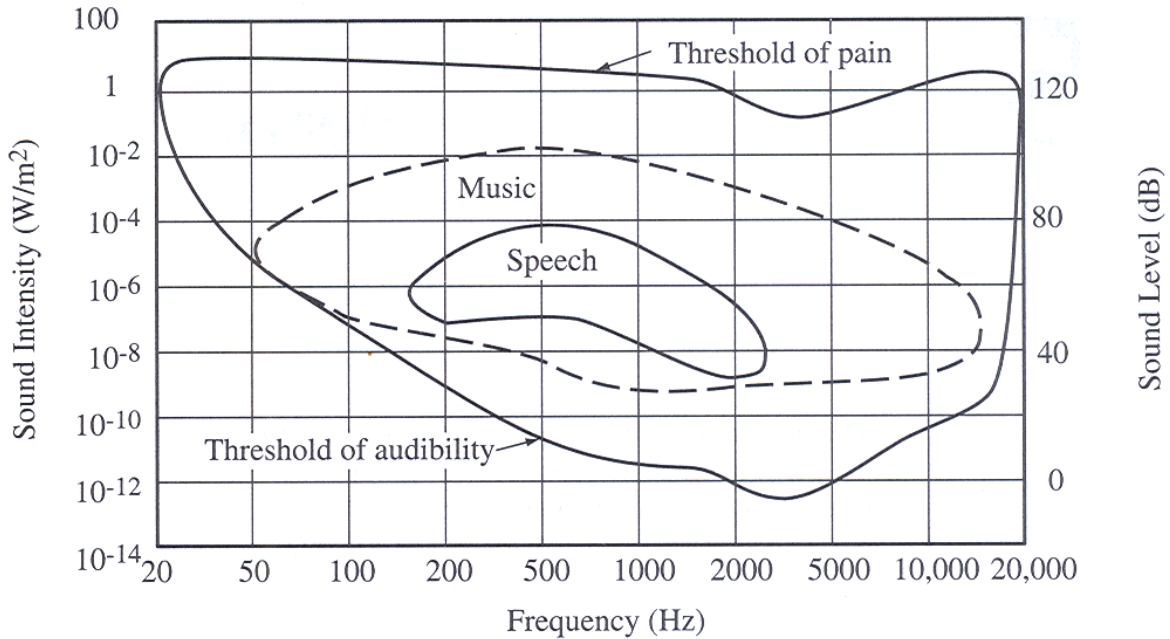
$$SIL = L_I \equiv 10 \log_{10} \left(\frac{I_{rms}}{I_{o rms}} \right) \text{ (dB)}$$

The unit of Loudness/Sound Intensity Level is the deci-Bel (*dB*) {*n.b.* deci = 10, *Bel* in honor of Alexander Graham Bell}.

Note that musicians have quantitatively defined six different loudness levels:

fortissimo	<i>fff</i>	$I = 10^{-2}$ RMS W/m ²	L_I (dB) = 100
	<i>ff</i>	10^{-3}	90
	<i>f</i>	10^{-4}	80
	<i>p</i>	10^{-6}	60
	<i>pp</i>	10^{-7}	50
pianissimo	<i>ppp</i>	10^{-8}	40

The Range of Human Hearing: Sound Intensity, Sound Intensity Level vs. Frequency:



Sound Pressure Level: $SPL = L_p$ = Sound Pressure Level (units = deci-Bels, *dB*)

$$SPL = L_p \equiv 10 \log_{10} \left(\frac{p_{rms}^2}{p_{o rms}^2} \right) = 10 \log_{10} \left(\frac{p_{rms}}{p_{o rms}} \right)^2 = 20 \log_{10} \left(\frac{p_{rms}}{p_{o rms}} \right) \text{ (dB)}$$