Maxima (*i.e.* total constructive interference, $p_{tot}^2 = p_{o_1}^2 + p_{o_2}^2$ occur when $\cos \delta = +1$, *i.e.* when: $\delta = 0, \pm 2\pi, \pm 4\pi, \pm 6\pi, \ldots = 2n\pi, n = 0, \pm 1, \pm 2, \pm 3, \ldots$ corresponding to $\Delta L/\lambda = d \sin \theta / \lambda = 0, \pm 1, \pm 2, \pm 3, \ldots = 2n/2 = n$, i.e. $\Delta L = d \sin \theta = 0\lambda, \pm 1\lambda, \pm 2\lambda, \pm 3\lambda, \ldots = 2n\lambda/2 = n\lambda$.

Minima (*i.e.* total destructive interference, $p_{tot}^2 = p_{o_1}^2 - p_{o_2}^2$ occur when $\cos \delta = -1$, *i.e.* when $\delta = \pm \pi, \pm 3\pi, \pm 5\pi, \pm 7\pi, \ldots = (2n+1)\pi, n = 0, \pm 1, \pm 2, \pm 3, \ldots$ corresponding to $\Delta L/\lambda = d \sin \theta / \lambda = \pm 1/2, \pm 3/2, \pm 5/2, \ldots = (2n+1)/2$, i.e. $\Delta L = d \sin \theta = \pm \lambda/2, \pm 3\lambda/2, \pm 5\lambda/2, \ldots = (2n+1)\lambda./2$.

As drawn in the above figure, this phasor diagram represents a "snapshot" in time – *i.e.* at some particular time *t*. As time *t* progresses, the entire phasor triangle precesses (i.e. rotates with angular frequency ω about its origin (the base point of over-pressure amplitude # 1)) in a <u>counter-clockwise</u> direction.

Note that the acoustical interference of two sound sources with each other -e.g. two loudspeakers - is the analog of Young's two-slit interference experiment in optics!

Note also that the sound intensity, $I(Watts/m^2)$ is proportional to the (modulus) square of the over-pressure amplitude $-i.e. I(z,t) \sim p^2(z,t)$. Thus, we can rewrite the above formula in terms of sound intensities: $I_{tot} = I_1 + I_2 + 2\sqrt{I_1}\sqrt{I_2} \cos \delta$.

The sound intensity distribution $I_{tot}(x)$ vs. $x (= \delta)$ = transverse distance (at z = L) is shown in below for equal intensities from two sound sources, $I_1 = I_2 = I_0 = 1$, when $I_{tot}(x) = 2I_0[1 + \cos(x)]$.



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