



$A$  = displacement amplitude of wave = max **displacement** from equilibrium position (meters,  $m$ )

$f$  = frequency of wave = number of complete cycles per second of wave  
(cycles per second = cps = Hertz, or Hz).

$\lambda$  = “lambda” = spatial wavelength of wave – distance to complete one oscillation cycle  
(meters,  $m$ )

$\tau$  = “tau” = period of wave = time to complete one oscillation cycle = “temporal wavelength”  
(seconds (secs, or s) ):

$$\tau = 1/f$$

$v$  = speed of propagation of wave (meters/second = m/s):  $v = f\lambda$

$\omega$  = “omega” = angular frequency (radians/second = rads/sec, or rads/s):

$$\omega = 2\pi f, \quad f = \omega/2\pi$$

$k$  = spatial wave number (inverse meters, i.e. 1/meters = 1/m):

$$k = 2\pi/\lambda$$

Hence, we also see that:  $v = f\lambda = 2\pi f \cdot \lambda/2\pi = \omega/k$

Sinusoidal **longitudinal** wave propagation {in the +ve  $z$ -direction} (relevant e.g. for sound propagation in air/water) is mathematically described by:

$$Z(z,t) = Z_o \sin(\omega t - kz)$$

where  $z$  = listener’s position,  $Z_o$  = longitudinal displacement amplitude (i.e. along the direction of propagation) and  $Z(z,t)$  is the instantaneous **longitudinal displacement** (i.e. longitudinal deviation) from the wave’s **equilibrium** position at the point  $z$  at time  $t$ .

Note that the **argument** of the sine function ( $\omega t - kz$ ) = **constant**. Thus, as time  $t$  increases, the position  $z$  must also increase – hence the name **traveling** wave. Hence, we also see that an argument of the sine function of the form ( $\omega t + kz$ ) = **constant** mathematically represents a traveling longitudinal displacement plane wave propagating in the  $-z$  direction:  $Z(z,t) = Z_o \sin(\omega t + kz)$ .