Some Examples of Physical Systems Exhibiting 1/f Noise:



Log Frequency

Fractional Brownian Motion, Fractional Brownian Noise

A dynamical system that obeys fractional Brownian noise (fBn), *e.g.* electrical noise in a carbon composition resistor, is a single-valued function of time V(t). The <u>increments</u> of the dynamical system from one moment to the next $\Delta V(\Delta t) = V(t_2) - V(t_1)$ obey a Gaussian probability distribution function (PDF):

$$f\left(\Delta V\left(\Delta t\right);\sigma_{\Delta V}\right) = \frac{1}{\sqrt{2\pi}\sigma_{\Delta V}}e^{-\Delta V^{2}(\Delta t)/2\pi\sigma_{\Delta V}^{2}}$$

The frequency-domain power spectral density (PSD) function $S_V(f)$ associated with the time-domain fluctuating quantity V(t) is a measure of the mean squared variation (*i.e.* variance) $\langle V^2(t) \rangle$ of V(t) in a unit bandwidth centered on the frequency f. Note that if the physical units of V(t) are *e.g. Volts*, the units of the PSD function $S_V(f)$ are *Volts*²/Hz.