

Thus:

$$\begin{aligned} V^{PSD_x}(\omega, t) &\equiv V^{Sig}(\omega, t) \otimes V^{Ref}(\omega, t) \\ &= \frac{1}{2} V_o^{Sig}(\omega) \cdot V_o^{Ref} \left[\cos \left\{ 2\omega t + (\varphi_S(\omega) + \varphi_R) \right\} + \cos \left\{ (\varphi_S(\omega) - \varphi_R) \right\} \right] \end{aligned}$$

and:

$$\begin{aligned} V^{PSD_y}(\omega, t) &\equiv V^{Sig}(\omega, t) \otimes V_{\pi/2}^{Ref}(\omega, t) \\ &= -\frac{1}{2} V_o^{Sig}(\omega) V_o^{Ref} \left[\sin \left\{ 2\omega t + (\varphi_S(\omega) + \varphi_R) \right\} - \sin \left\{ (\varphi_S(\omega) - \varphi_R) \right\} \right] \end{aligned}$$

Next, we (deliberately) choose to set the **reference** amplitude to: $V_o^{Ref} \equiv \sqrt{2} = 1.4142 \text{ Volts}$
 {i.e. set the **RMS reference** amplitude to: $V_{o_{RMS}}^{Ref} \equiv \frac{1}{\sqrt{2}} V_o^{Ref} = 1.0000 \text{ Volts}$ }.

Then, the two **PSD product** signals become:

$$\begin{aligned} V^{PSD_x}(\omega, t) &\equiv V^{Sig}(\omega, t) \otimes V^{Ref}(\omega, t) \\ &= +\frac{1}{\sqrt{2}} V_o^{Sig}(\omega) \left[\cos \left\{ 2\omega t + (\varphi_S(\omega) + \varphi_R) \right\} + \cos \left\{ (\varphi_S(\omega) - \varphi_R) \right\} \right] \end{aligned}$$

and:

$$\begin{aligned} V^{PSD_y}(\omega, t) &\equiv V^{Sig}(\omega, t) \otimes V_{\pi/2}^{Ref}(\omega, t) \\ &= -\frac{1}{\sqrt{2}} V_o^{Sig}(\omega) \left[\sin \left\{ 2\omega t + (\varphi_S(\omega) + \varphi_R) \right\} - \sin \left\{ (\varphi_S(\omega) - \varphi_R) \right\} \right] \end{aligned}$$

Thus, note that the **RMS** output signal amplitude is: $V_{o_{RMS}}^{Sig}(\omega) \equiv \frac{1}{\sqrt{2}} V_o^{Sig}(\omega)$

Thus, the two **PSD product** signals can be expressed in terms of their **RMS** amplitudes as:

$$\begin{aligned} V^{PSD_x}(\omega, t) &\equiv V^{Sig}(\omega, t) \otimes V^{Ref}(\omega, t) \\ &= V_{o_{RMS}}^{Sig}(\omega) \left[\cos \left\{ 2\omega t + (\varphi_S(\omega) + \varphi_R) \right\} + \cos \left\{ (\varphi_S(\omega) - \varphi_R) \right\} \right] \end{aligned}$$

and:

$$\begin{aligned} V^{PSD_y}(\omega, t) &\equiv V^{Sig}(\omega, t) \otimes V_{\pi/2}^{Ref}(\omega, t) \\ &= -V_{o_{RMS}}^{Sig}(\omega) \left[\sin \left\{ 2\omega t + (\varphi_S(\omega) + \varphi_R) \right\} - \sin \left\{ (\varphi_S(\omega) - \varphi_R) \right\} \right] \end{aligned}$$