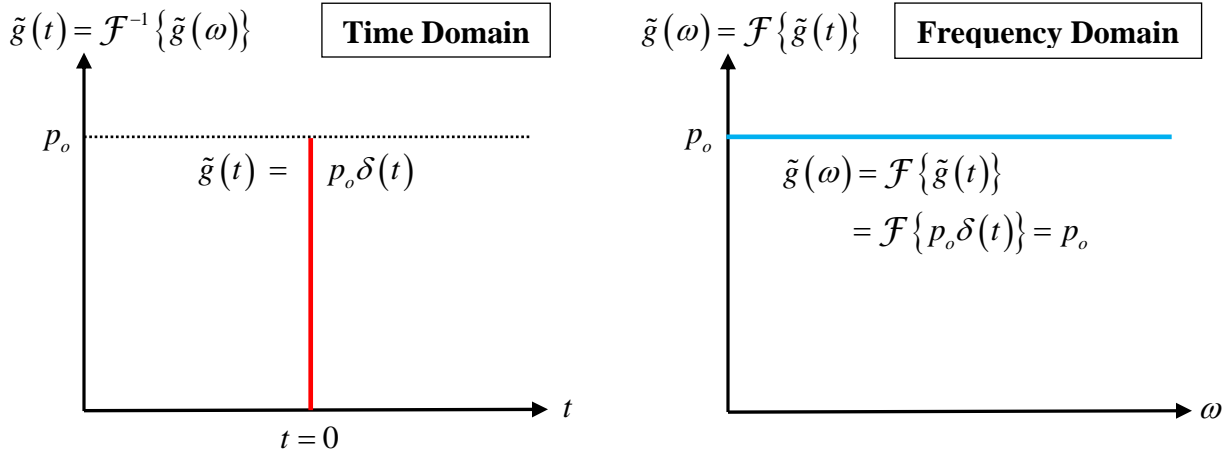


Conversely, an infinitely sharp/narrow **time domain** sound “spike”  $\tilde{g}_1(t) = p_o \delta(t)$  (*Pascals/sec*) produces a **flat** frequency **spectrum** (a **continuum** of frequencies with **equal** amplitudes)  $\tilde{g}(f) = \tilde{g}(\omega) = \mathcal{F}\{\tilde{g}(t)\} = p_o$  (*Pascals*), as shown graphically in the two figures below:



There are many useful relations associated with Fourier transforms, which we summarize below, for the most commonly used ones:

<u>Time-Domain:</u>	<u>Frequency Domain:</u>
<b>Linearity:</b> $\tilde{h}(t) = a\tilde{f}(t) + b\tilde{g}(t) \Rightarrow$	$\tilde{h}(\omega) = a\tilde{f}(\omega) + b\tilde{g}(\omega)$
<b>Translation:</b> $\tilde{h}(t) = \tilde{f}(t - t_o) \Rightarrow$	$\tilde{h}(\omega) = \tilde{f}(\omega) e^{i\omega t_o}$
<b>Modulation:</b> $\tilde{h}(t) = \tilde{f}(t) e^{i\omega_o t} \Rightarrow$	$\tilde{h}(\omega) = \tilde{f}(\omega - \omega_o)$
<b>Scaling:</b> $\tilde{h}(t) = \tilde{f}(at) \Rightarrow$	$\tilde{h}(\omega) = \frac{1}{ a } \tilde{f}\left(\frac{\omega}{a}\right)$
<b>Conjugation:</b> $\tilde{h}(t) = \tilde{f}^*(t) \Rightarrow$	$\tilde{h}(\omega) = \tilde{f}^*(-\omega)$