

The over-pressure ***difference*** signal is input to an ***integrating*** op-amp, which electronically carries out the above integral operation. The voltage signal output from the integrating op-amp is thus ***proportional*** to the 1-D particle velocity $\tilde{u}_r(\vec{r}, t) = \tilde{u}_r\left(\frac{1}{2}(\vec{r}_1 + \vec{r}_2), t\right)$! Using 3 such microphone pairs (in orthogonal x - y - z orientation) thus yields the full 3-D particle velocity $\tilde{\vec{u}}(\vec{r}, t)$!

The use of matched pairs of omni-directional pressure microphones separated by a small distance $\Delta z \ll \lambda$ to measure the local pressure gradient $\Delta_z \tilde{p}(\vec{r}, t) / \Delta z$ and thereby infer (*i.e.* compute) the local 1-D particle velocity $\partial \tilde{u}_z(\vec{r}, t) / \partial t$ is known as the so-called ***p-p method***.

If the diaphragm of the pressure microphone is ***fully-open*** (*i.e.* not enclosed), such a microphone {of characteristic longitudinal/ z -dimension d } measures the local over-pressure ***difference*** $\Delta \tilde{p}_{dia}(\vec{r}, t) = \tilde{p}_{dia}^{front}(\vec{r}, t) - \tilde{p}_{dia}^{rear}(\vec{r}, t)$ for $d \ll \lambda$ - *i.e.* it becomes a ***differential-pressure*** microphone. Furthermore, it is obvious that differential pressure microphones have a vectorial-type directional response, since the voltage signal output from this microphone will reverse its sign if the differential microphone is rotated about its symmetry axis by 180° . The angular response of a differential pressure microphone is therefore vectorially described by $\Delta \tilde{p}_{dia}(\vec{r}, t) \hat{n}$ where \hat{n} is defined as the ***outward*** pointing unit vector from the front surface of the microphone diaphragm. For a sound wave with vector wavenumber $\vec{k} = |\vec{k}| \hat{k} = k \hat{k}$ ($\hat{k} \parallel$ to the propagation direction), the ***angular*** response of the differential pressure microphone is $\Delta \tilde{p}_{dia}(\vec{r}, t) \hat{n} \cdot \hat{k} = \Delta \tilde{p}_{dia}(\vec{r}, t) \cos \Theta$ where Θ is the 3-D opening angle between \hat{n} and \hat{k} .

Thus when: $\Theta = 0^\circ$, $\hat{n} \cdot \hat{k} = \cos \Theta = +1$ and: $\Delta \tilde{p}_{dia}(\vec{r}, t) \hat{n} \cdot \hat{k} = +\Delta \tilde{p}_{dia}(\vec{r}, t)$.

When: $\Theta = 90^\circ$, $\hat{n} \cdot \hat{k} = \cos \Theta = 0$ and: $\Delta \tilde{p}_{dia}(\vec{r}, t) \hat{n} \cdot \hat{k} = 0$.

When: $\Theta = 180^\circ$, $\hat{n} \cdot \hat{k} = \cos \Theta = -1$ and: $\Delta \tilde{p}_{dia}(\vec{r}, t) \hat{n} \cdot \hat{k} = -\Delta \tilde{p}_{dia}(\vec{r}, t)$.

The polar response of a ***differential*** pressure microphone is a ***figure-8 pattern***, as shown below:

