

The **magnitude** of the complex velocity amplitude  $\tilde{v}_o(\omega)$  of the microphone diaphragm is:

$$|\tilde{v}_o(\omega)| \equiv \sqrt{v_{or}^2(\omega) + v_{oi}^2(\omega)} = \omega \left( \frac{p_o A_{dia}}{m_{dia}} \right) \frac{1}{\sqrt{(\omega_o^2 - \omega^2)^2 + \omega^2 \gamma_{dia}^2}}$$

If we again define  $x(\omega) \equiv \omega/\omega_o$  and  $y \equiv \gamma_{dia}/\omega_o$  then we can rewrite the {normalized} magnitude of the complex velocity amplitude  $\tilde{v}_o(\omega)$  and  $v$ -phase as:

$$v\text{-Res}(x(\omega)) \equiv \frac{\omega_o |\tilde{v}_o(\omega)|}{\left( \frac{p_o A_{dia}}{m_{dia}} \right)} = \frac{\left( \frac{\omega}{\omega_o} \right)}{\sqrt{\left[ 1 - \left( \frac{\omega}{\omega_o} \right)^2 \right]^2 + \left( \frac{\omega}{\omega_o} \right)^2 \left( \frac{\gamma_{dia}}{\omega_o} \right)^2}} = \frac{x}{\sqrt{(1-x^2)^2 + x^2 y^2}}$$

$$\varphi_v(\omega) = \tan^{-1} \left( \frac{(\omega_o^2 - \omega^2)}{\omega \gamma_{dia}} \right) = \tan^{-1} \left( \frac{1 - \left( \frac{\omega}{\omega_o} \right)^2}{\left( \frac{\omega}{\omega_o} \right) \left( \frac{\gamma_{dia}}{\omega_o} \right)} \right) = \tan^{-1} \left( \frac{1-x^2}{x \cdot y} \right)$$

We again have the usual three conditions of **underdamped**, **critically damped** and **overdamped** motion for  $y \equiv \gamma_{dia}/\omega_o \ll 1$ ,  $y \equiv \gamma_{dia}/\omega_o = 1$  and  $y \equiv \gamma_{dia}/\omega_o \gg 1$ , respectively. The following two color-coded figures show normalized  $v$ -Res( $x$ ) vs.  $x$  and  $v$ -Phase( $x$ ) vs.  $x$  for  $y = 0.05$  (pink), 1.0 (cyan) and 10.0 (violet):

