

From the above two figures, we see that if we **overdamp** the diaphragm of the microphone ( $y \equiv \gamma_{dia}/\omega_o = 10$ , violet curves), we achieve a region of flat frequency response, albeit with **non-constant** phase shift over the {fractional} frequency range  $0.01 \leq x(\omega) \equiv \omega/\omega_o \leq 100$ . These response curves are relevant for the design of microphones whose output signal response  $\tilde{V}_{mic}(t)$  to an over-pressure  $\tilde{p}(\vec{r}, t)$  that is linearly proportional to the **displacement** of the diaphragm,  $\tilde{x}_{dia}(t)$  - e.g. **electret condenser-type** microphones.

The output responses of **dynamic** and **ribbon-type** microphones to an over-pressure  $\tilde{p}(t)$  are linearly proportional to the **velocity** of the diaphragm of the microphone,  $\tilde{v}_{dia}(t) = \partial\tilde{x}_{dia}(t)/\partial t$ , since e.g. a time-varying *EMF* (i.e. voltage)  $\tilde{\epsilon}_{mic}(t) = |\tilde{v}_{dia}(t)| \cdot |\vec{B}_o| \cdot \ell_{ribbon}$  {where  $\ell_{ribbon}(m)$  is the length of the metal ribbon} is produced across the top/bottom of the corrugated metal ribbon diaphragm due to the instantaneous differential over-pressure  $\Delta\tilde{p}_{ribbon}(t)$  acting on it.

We have already seen that a harmonically-varying overpressure amplitude at the diaphragm of the microphone  $\tilde{p}(t) = p_o e^{i\omega t}$  results in a harmonically-varying displacement of the microphone  $\tilde{x}_{dia}(t) = \tilde{x}_o(\omega) e^{i\omega t}$ . Thus  $\tilde{v}_{dia}(t) = \partial\tilde{x}_{dia}(t)/\partial t = i\omega\tilde{x}_o(\omega) e^{i\omega t} = i\omega\tilde{x}_{dia}(t)$ , i.e. the velocity of the diaphragm  $\tilde{v}_{dia}(t)$  is  $+90^\circ$  ahead in phase relative to the displacement of the diaphragm,  $\tilde{x}_{dia}(t)$  and is also linearly proportional to the (angular) frequency  $\omega = 2\pi f$ . We also see that  $\tilde{v}_{dia}(t) = \partial\tilde{x}_{dia}(t)/\partial t = i\omega\tilde{x}_o(\omega) e^{i\omega t} = i\omega\tilde{x}_{dia}(t) = \tilde{v}_o(\omega) e^{i\omega t}$  and hence that  $\tilde{v}_o(\omega) = i\omega\tilde{x}_o(\omega)$ . Thus the complex velocity amplitude of the diaphragm of a microphone is:

$$\tilde{v}_o(\omega) = i\omega\tilde{x}_o(\omega) = i\omega \left( \frac{p_o A_{dia}}{m_{dia}} \right) \frac{[(\omega_o^2 - \omega^2) - i\omega\gamma_{dia}]}{(\omega_o^2 - \omega^2)^2 + \omega^2\gamma_{dia}^2} = \omega \left( \frac{p_o A_{dia}}{m_{dia}} \right) \frac{[\omega\gamma_{dia} + i(\omega_o^2 - \omega^2)]}{(\omega_o^2 - \omega^2)^2 + \omega^2\gamma_{dia}^2}$$

The **real/in-phase component** of the velocity amplitude  $\tilde{v}_o(\omega)$  of the microphone diaphragm is:

$$v_{or}(\omega) \equiv \text{Im}\{\tilde{v}_o(\omega)\} = \omega \left( \frac{p_o A_{dia}}{m_{dia}} \right) \frac{\omega\gamma_{dia}}{(\omega_o^2 - \omega^2)^2 + \omega^2\gamma_{dia}^2}$$

The **imaginary/quadrature component** of the velocity amplitude  $\tilde{v}_o(\omega)$  of the microphone diaphragm is:

$$v_{oi}(\omega) \equiv \text{Re}\{\tilde{v}_o(\omega)\} = \omega \left( \frac{p_o A_{dia}}{m_{dia}} \right) \frac{(\omega_o^2 - \omega^2)}{(\omega_o^2 - \omega^2)^2 + \omega^2\gamma_{dia}^2}$$

The **phase** of the velocity amplitude  $\tilde{v}_o(\omega)$  of the microphone diaphragm is:

$$\varphi_v(\omega) \equiv \tan^{-1} \left( \frac{\text{Im}\{\tilde{v}_o(\omega)\}}{\text{Re}\{\tilde{v}_o(\omega)\}} \right) = \tan^{-1} \left( \frac{(\omega_o^2 - \omega^2)}{\omega\gamma_{dia}} \right)$$