

The complex sound field  $\tilde{S}(\vec{r}, t)$  associated with a “point” monopole sound source radiating monochromatic, radially-outgoing spherical waves thus has **three** basic regions, or zones:

- (a) **The “near” zone:**  $kr \ll 1$ , the radial particle velocity  $\tilde{u}_r(r, t) \sim -i|\tilde{B}|/z_o kr^2$  is largely **imaginary** (i.e. **reactive**), decreasing as  $\sim 1/r^2$  (while the pressure  $\tilde{p}(r, t) \sim |\tilde{B}|/r$  decreases as  $\sim 1/r$ ), and where the particle velocity **lags** the pressure by  $\varphi_p - \varphi_u = \tan^{-1}(1/kr) \sim \tan^{-1}(\infty) \sim 90^\circ$  in phase. This region of the complex sound field  $\tilde{S}(\vec{r}, t)$  is **reactive**, largely consisting of **non-propagating** acoustic energy, and is also **inertia**-like (i.e. **mass**-like), because  $u_{r,i}(r) = \text{Im}\{\tilde{u}_r(r)\} < 0$  for  $kr \ll 1$ .
- (b) **The “intermediate” zone:**  $kr \sim 1$ , the radial particle velocity  $\tilde{u}_r(r, t) \sim (1-i)|\tilde{B}|/2z_or$  has  $\sim$  comparable **real** and **imaginary** components, decreasing somewhat/slightly faster than  $\sim 1/r$  (while the pressure  $\tilde{p}(r, t) \sim |\tilde{B}|/r$  decreases as  $\sim 1/r$ ), and where the particle velocity **lags** the pressure by  $\varphi_p - \varphi_u = \tan^{-1}(1/kr) \sim \tan^{-1}(1) \sim 45^\circ$  in phase. This region of the complex sound field  $\tilde{S}(\vec{r}, t)$  is  $\sim$  an **equal** mix of **propagating** and **non-propagating** acoustic energy.
- (c) **The “far” (or radiation) zone:**  $kr \gg 1$ , the radial particle velocity  $\tilde{u}_r(r, t) \sim 1|\tilde{B}|/z_or$  is largely **real** (i.e. **active**), decreasing  $\sim 1/r$  (while the pressure  $\tilde{p}(r, t) \sim |\tilde{B}|/r$  also decreases as  $\sim 1/r$ ), and where the radial particle velocity is **in-phase** with the pressure, i.e.  $\varphi_p - \varphi_u = \tan^{-1}(1/kr) \sim \tan^{-1}(0) \sim 0^\circ$ . This region of the complex sound field  $\tilde{S}(\vec{r}, t)$  is **active**, dominated by **propagating** acoustic energy.

The radial complex **specific** acoustic impedance and its magnitude are:

$$\tilde{z}_{a_r}(r, \omega) \equiv \frac{\tilde{p}(r, \omega)}{\tilde{u}_r(r, \omega)} = z_o \frac{1}{[1-i/kr]} = z_o \frac{[1+i/kr]}{[1+(1/kr)^2]} \quad \text{and:} \quad |\tilde{z}_{a_r}(r, \omega)| = z_o \frac{\sqrt{1+(1/kr)^2}}{[1+(1/kr)^2]} = z_o \frac{1}{\sqrt{1+(1/kr)^2}}$$

Note that since  $\tilde{z}_{a_r}(r, \omega) = \rho_o \tilde{c}_{a_r}(r, \omega)$  these relations can be written in dimensionless form as:

$$\frac{\tilde{z}_{a_r}(r, \omega)}{z_o} = \frac{[1+i/kr]}{[1+(1/kr)^2]} = \frac{\tilde{c}_{a_r}(r, \omega)}{c} \quad \text{and:} \quad \frac{|\tilde{z}_{a_r}(r, \omega)|}{z_o} = \frac{1}{\sqrt{1+(1/kr)^2}} = \frac{|\tilde{c}_{a_r}(r, \omega)|}{c}$$

The real and imaginary parts of the complex radial **specific** acoustic impedance associated with the point monopole sound source are thus:

$$z_{a_r}^r(r, \omega) = \text{Re}\{\tilde{z}_{a_r}(r, \omega)\} = z_o \frac{1}{[1+(1/kr)^2]} \quad \text{and:} \quad z_{a_r}^i(r, \omega) = \text{Im}\{\tilde{z}_{a_r}(r, \omega)\} = z_o \frac{1/kr}{[1+(1/kr)^2]}$$