

## Acoustic Reflectance/Transmittance/Absorbance and Acoustic Reflection/Transmission/Absorption Coefficients:

The physical meaning of the complex quantity  $\tilde{R} \equiv \tilde{B}/\tilde{A} = |\tilde{R}|e^{i\Delta\phi_{RA}}$  used in (all of) the above formulae for this two counter-propagating monochromatic plane waves problem can also be used to describe various other types of acoustical physics situations, *e.g.* by interpreting  $\tilde{R}$  as the **complex acoustic reflectance** associated with a sound wave reflecting off of a surface. The {purely real} **reflection coefficient** associated with the surface is then defined as:  $0 \leq R \equiv |\tilde{R}|^2 = \tilde{R} \cdot \tilde{R}^* \leq 1$ .

If a sound wave is only partially reflected from a surface, then it is either partially transmitted (with complex acoustic **transmittance**  $\tilde{T}$  and corresponding {purely real} **transmission coefficient**  $0 \leq T \equiv |\tilde{T}|^2 = \tilde{T} \cdot \tilde{T}^* \leq 1$ ) and/or is absorbed by the surface (with complex acoustic **absorbance**  $\tilde{A}$  and corresponding {purely real} **absorption coefficient**  $0 \leq A \equiv |\tilde{A}|^2 = \tilde{A} \cdot \tilde{A}^* \leq 1$ ), since we **must** have (by conservation of energy at the surface/interface):  $R + T + A = 1$ .

### Limiting/Special Cases of Interest:

1.) A single monochromatic traveling plane wave (emitted from a sound source *e.g.* located at  $x = -\infty$ ) propagating in the +ve  $x$ -direction and reflects, at normal incidence, off of a **rigid, perfectly reflecting** infinite plane (*e.g.* located at  $x = x_o > 0$ ), thereby producing a reflected wave (of **equal** amplitude) that propagates in the -ve  $x$ -direction. This situation corresponds to  $\tilde{R} = |\tilde{R}|e^0 = +1$  at  $x = x_o > 0$ , which has the associated boundary condition  $\tilde{p}_{refl}(x = x_o, t) = \tilde{p}_{inc}(x = x_o, t)$ , *i.e.* **no** phase change occurs upon reflection, such that an over-pressure **anti-node** exists at  $x = x_o > 0$ :

$$\tilde{p}_{tot}(x = x_o, t) = \tilde{p}_{inc}(x = x_o, t) + \tilde{p}_{refl}(x = x_o, t) = 2\tilde{p}_{inc}(x = x_o, t).$$

2.) A single monochromatic traveling plane wave (emitted from a sound source *e.g.* located at  $x = -\infty$ ) propagating in the +ve  $x$ -direction and reflects, at normal incidence, off of an infinite **pressure-release** plane consisting of an air-water interface (located at  $x = x_o > 0$ ), thereby producing a reflected wave (of equal amplitude) that propagates in the -ve  $x$ -direction.

This situation corresponds to  $\tilde{R} = |\tilde{R}|e^{i\pi} = -1$ . An air-water interface (*n.b.* “viewed” from the water side) closely approximates an **ideal pressure-release surface**, for which the boundary condition at the pressure-release surface is  $\tilde{p}_{refl}(x = x_o, t) = -\tilde{p}_{inc}(x = x_o, t)$  (*i.e.* a phase change of  $180^\circ$  occurs upon reflection), such that an over-pressure **node** exists at  $x = x_o > 0$ :

$$\tilde{p}_{tot}(x = x_o, t) = \tilde{p}_{inc}(x = x_o, t) - \tilde{p}_{refl}(x = x_o, t) = 0.$$