

$$\begin{aligned}\langle w_{tot}(x=0,t) \rangle_t &\equiv \langle w_{potl}(x=0) \rangle_t + \langle w_{kin}(x=0) \rangle_t \\ &= \frac{1}{2} \frac{|\tilde{A}|^2}{\rho_o c^2} [1 + \cancel{\cos \Delta \varphi_{BA}^o}] + \frac{1}{2} \frac{|\tilde{A}|^2}{\rho_o c^2} [1 - \cancel{\cos \Delta \varphi_{BA}^o}] = \frac{|\tilde{A}|^2}{\rho_o c^2} = \frac{|\tilde{A}|^2}{z_o c}\end{aligned}$$

When: $\Delta \varphi_{BA} = 0, \pm 2\pi, \pm 4\pi, \pm 6\pi, \dots = \pm n_{even} \pi$ the energy density is all **potential** energy density:

$$\langle w_{potl}(x=0,t) \rangle_t = \frac{1}{2} \frac{\langle p_{tot}^2(x=0,t) \rangle_t}{\rho_o c^2} = \frac{1}{2} \frac{|\tilde{A}|^2}{\rho_o c^2} [1 + \cos(\pm n_{even} \pi)] = \frac{|\tilde{A}|^2}{\rho_o c^2}$$

$$\langle w_{kin}(x=0,t) \rangle_t = \frac{1}{2} \rho_o \langle u_{tot}^2(x=0,t) \rangle_t = \frac{1}{2} \frac{|\tilde{A}|^2}{\rho_o c^2} [1 - \cos(\pm n_{even} \pi)] = 0$$

$$\langle w_{tot}(x=0,t) \rangle_t \equiv \langle w_{potl}(x=0,t) \rangle_t + \langle w_{kin}(x=0,t) \rangle_t = \frac{|\tilde{A}|^2}{\rho_o c^2} + 0 = \frac{|\tilde{A}|^2}{\rho_o c^2} = \frac{|\tilde{A}|^2}{z_o c}$$

When: $\Delta \varphi_{AB} = \pm 1\pi, \pm 3\pi, \pm 5\pi, \dots = \pm n_{odd} \pi$ the energy density is all **kinetic** energy density:

$$\langle w_{potl}(x=0,t) \rangle_t = \frac{1}{2} \frac{\langle p_{tot}^2(x=0,t) \rangle_t}{\rho_o c^2} = \frac{1}{2} \frac{|\tilde{A}|^2}{\rho_o c^2} [1 + \cos(\pm n_{odd} \pi)] = 0$$

$$\langle w_{kin}(x=0,t) \rangle_t = \frac{1}{2} \rho_o \langle u_{tot}^2(x=0,t) \rangle_t = \frac{1}{2} \frac{|\tilde{A}|^2}{\rho_o c^2} [1 - \cos(\pm n_{odd} \pi)] = \frac{|\tilde{A}|^2}{\rho_o c^2}$$

$$\langle w_{tot}(x=0,t) \rangle_t \equiv \langle w_{potl}(x=0,t) \rangle_t + \langle w_{kin}(x=0,t) \rangle_t = 0 + \frac{|\tilde{A}|^2}{\rho_o c^2} = \frac{|\tilde{A}|^2}{\rho_o c^2} = \frac{|\tilde{A}|^2}{z_o c}$$

We coded up the above acoustic expressions in Matlab to obtain plots of them vs. dimensionless position, $\theta = kx$ for various values of $0 \leq |\tilde{R}| \leq 1$ for two counter-propagating 1-D monochromatic traveling plane waves and posted a write-up along with the Matlab *.m script on the Physics 406 Software web-page: http://courses.physics.illinois.edu/phys406/406pom_sw.html