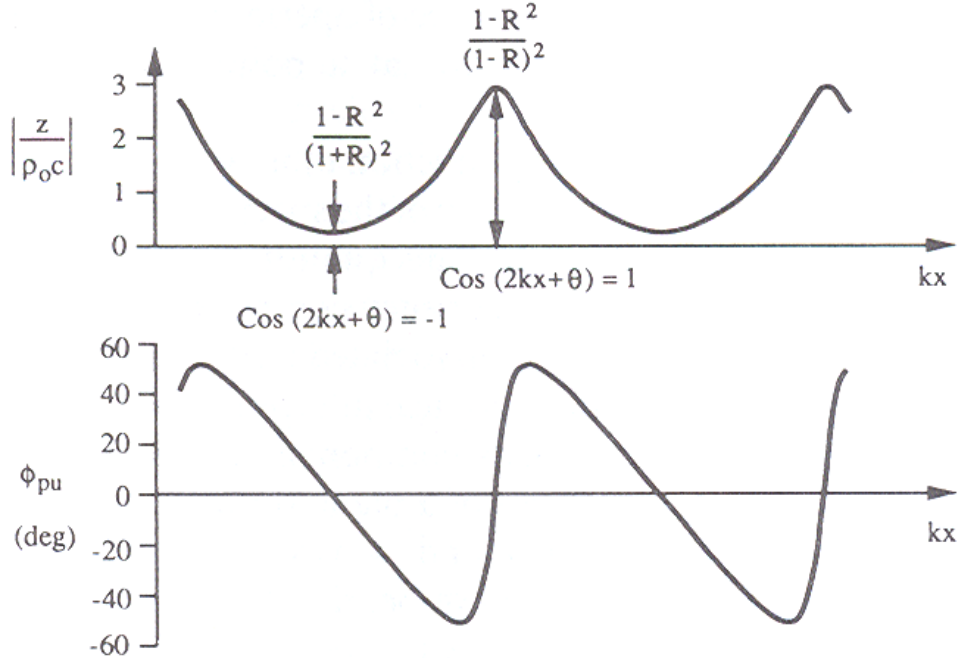


A perhaps somewhat more general situation associated with two counter-propagating monochromatic plane waves in “*free air*”, is e.g. the case when $|\tilde{R}| \equiv |\tilde{B}|/|\tilde{A}| = 0.5$ and $\Delta\phi_{BA}^o = 0.5$; the {normalized} magnitude of the complex longitudinal **specific** acoustic impedance $|\tilde{z}_{tot}^{\parallel}(x)|/z_o = |\tilde{z}_{tot}^{\parallel}(x)|/\rho_o c$ and its phase $\phi_z(x) = \Delta\phi_{p_{tot}-u_{tot}^{\parallel}}(x) = \phi_{p_{tot}}(x) - \phi_{u_{tot}^{\parallel}}(x)$ vs. kx are shown in the figure(s) below.



The complex **frequency-domain** total/resultant complex longitudinal sound intensity associated with two counter-propagating monochromatic plane waves in “*free air*”, with $k = \omega/c$ is:

$$\begin{aligned}
 \tilde{I}_{a_{tot}}^{\parallel}(x, \omega) &\equiv \frac{1}{2} \tilde{p}_{tot}(x, \omega) \cdot \tilde{u}_{tot}^{\parallel*}(x, \omega) \\
 &= \frac{1}{2} \tilde{A} \left[1 + |\tilde{R}| e^{i(2kx + \Delta\phi_{BA}^o)} \right] e^{-i(\omega t - kx)} \cdot \frac{\tilde{A}^*}{\rho_o c} \left[1 - |\tilde{R}| e^{-i(2kx + \Delta\phi_{BA}^o)} \right] e^{-i(\omega t - kx)} \\
 &= \frac{1}{2} \frac{|\tilde{A}|^2}{\rho_o c} \left[1 + |\tilde{R}| e^{i(2kx + \Delta\phi_{BA}^o)} \right] \cdot \left[1 - |\tilde{R}| e^{-i(2kx + \Delta\phi_{BA}^o)} \right] \\
 &= \frac{1}{2} \frac{|\tilde{A}|^2}{\rho_o c} \left[1 + |\tilde{R}| \left\{ e^{i(2kx + \Delta\phi_{BA}^o)} - e^{-i(2kx + \Delta\phi_{BA}^o)} \right\} - |\tilde{R}|^2 \right] \quad \text{and using: } z_o \equiv \rho_o c \\
 &= \frac{1}{2} \frac{|\tilde{A}|^2}{z_o} \left[1 + 2i |\tilde{R}| \sin(2kx + \Delta\phi_{BA}^o) - |\tilde{R}|^2 \right] = \frac{1}{2} \frac{|\tilde{A}|^2}{z_o} \left[\left\{ 1 - |\tilde{R}|^2 \right\} + 2i |\tilde{R}| \sin(2kx + \Delta\phi_{BA}^o) \right]
 \end{aligned}$$