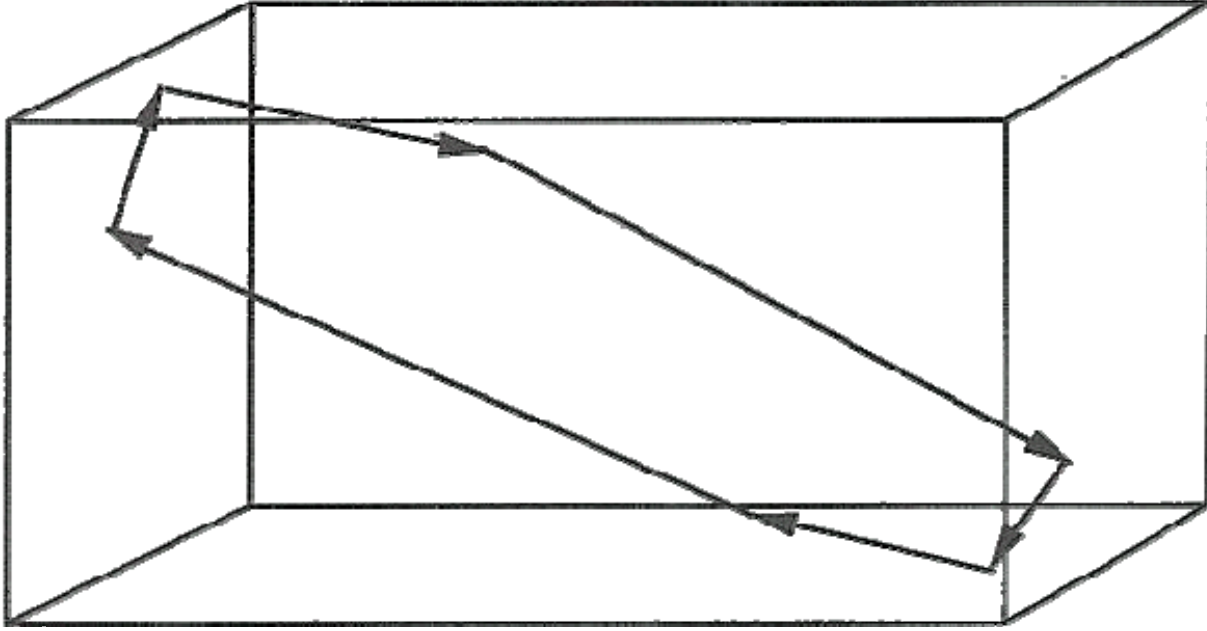


The third type of standing wave in a room are known as 3-D oblique modes, in which all six surfaces of the room are involved in producing standing waves, one such path is shown in the figure below:



For oblique modes, none of the $[xyz] = [lmn]$ indices are zero, and hence the eigen-frequencies associated with oblique modes are given by the full 3-D formula

$$f_{lmn} = \frac{1}{2} v \sqrt{\left(\frac{l}{L_x}\right)^2 + \left(\frac{m}{L_y}\right)^2 + \left(\frac{n}{L_z}\right)^2} \text{ with wavelength for the 3-D oblique modes of}$$

$$\lambda_{lmn} = 2 / \sqrt{\left(\frac{l}{L_x}\right)^2 + \left(\frac{m}{L_y}\right)^2 + \left(\frac{n}{L_z}\right)^2} .$$

The 3-D longitudinal displacement amplitudes for the oblique-mode resonances in this room / auditorium are of the form:

$$\xi_{lmn}(x, y, z, t) = U_{lmn}(x, y, z) T_{lmn}(t) = X_l(x) Y_m(y) Z_n(z) T_{lmn}(t)$$

$$\xi_{lmn}(x, y, z, t) = A_{lmn} \sin(k_l x) \sin(k_m y) \sin(k_n z) e^{i(\omega_{lmn} t + \phi_{lmn})}$$

$$\xi_{lmn}(x, y, z, t) = A_{lmn} \sin(l\pi x / L_x) \sin(m\pi y / L_y) \sin(n\pi z / L_z) e^{i(\omega_{lmn} t + \phi_{lmn})}$$

$$l, m, n = 1, 2, 3, 4, 5, \dots$$

whereas the 3-D over-pressure amplitude for oblique-mode resonances in this room/auditorium are of the form:

$$p_{lmn}(x, y, z, t) = V_{lmn}(x, y, z) T_{lmn}(t) = F_l(x) G_m(y) H_n(z) T_{lmn}(t)$$

$$p_{lmn}(x, y, z, t) = C_{lmn} \cos(k_l x) \cos(k_m y) \cos(k_n z) e^{i(\omega_{lmn} t + \phi_{lmn})}$$

$$p_{lmn}(x, y, z, t) = C_{lmn} \cos(l\pi x / L_x) \cos(m\pi y / L_y) \cos(n\pi z / L_z) e^{i(\omega_{lmn} t + \phi_{lmn})}$$

$$l, m, n = 1, 2, 3, 4, 5, \dots$$