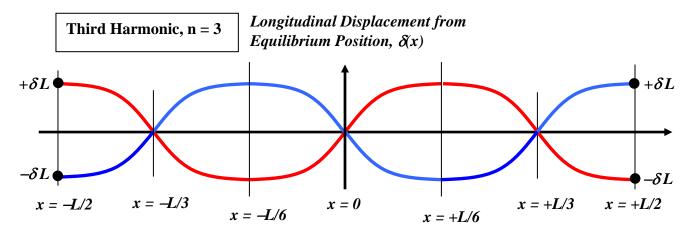
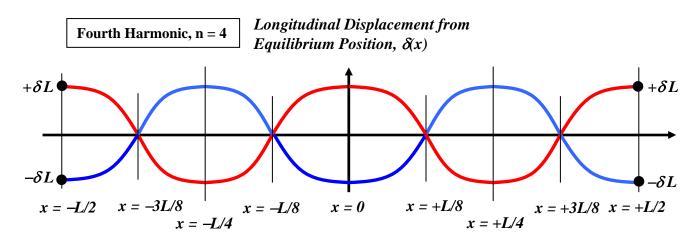
(*i.e.* one octave above) since the wavelength,  $\lambda_2 = L$  for this mode of vibration of the rod is half that of the wavelength,  $\lambda_1 = 2L$  associated with the fundamental mode. This mode of vibration of the rod has two nodes, located at  $x = \pm^{1}/_{4} L$  and three anti-nodes, one located at the mid-point of the rod at x = 0, and at the two ends of the rod, at  $x = \pm^{1}/_{2} L$ .

The next higher, third harmonic mode of vibration of the rod (n = 3) is shown in the figure below. The frequency  $f_3$  is three times higher than that of the fundamental frequency,  $f_1$ , since the wavelength,  $\lambda_3 = \frac{2}{3L}$  for this mode of vibration of the rod is one third of that of the wavelength,  $\lambda_1 = 2L$  associated with the fundamental mode. This mode of vibration of the rod has three nodes, one node located at x = 0, and two others located at  $x = \pm \frac{1}{3}L$ . This mode of vibration has four anti-nodes, two located at  $x = \pm \frac{1}{6}L$  and two located at the ends of the rod, at  $x = \pm \frac{1}{2}L$ .



The next higher, fourth harmonic mode of vibration of the rod (n = 4) is shown in the figure below. The frequency  $f_4$  is four times (i.e. two octaves) higher than that of the fundamental frequency,  $f_1$ , since the wavelength,  $\lambda_4 = 2/4L = \frac{1}{2}L$  for this mode of vibration of the rod is one fourth of that of the wavelength,  $\lambda_1 = 2L$  associated with the fundamental mode. This mode of vibration of the rod has four nodes, two nodes located at  $x = \pm 1/8 L$ , and two others located at  $x = \pm 3/8 L$ . There are five anti-nodes, one located at x = 0, two located at  $x = \pm 1/4 L$  and two located at the endpoints, at  $x = \pm 1/2 L$ .



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