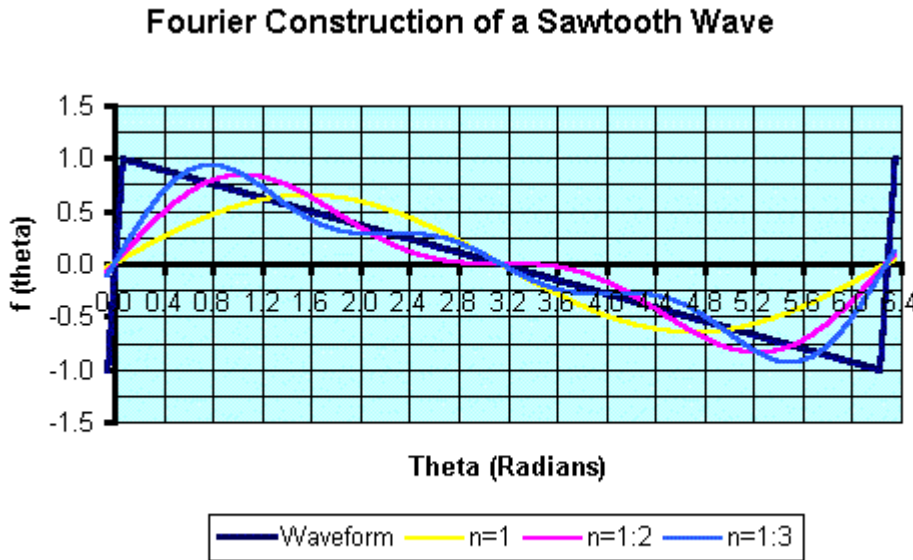


The following two figures show the “Fourier construction” of a periodic, bipolar, unit-amplitude sawtooth wave. The waveforms in these figures were generated using truncated, finite-term version(s) of the Fourier series expansion for this waveform:

$$f(\theta) \Big|_{\substack{\text{sawtooth} \\ \text{-wave}}} = \sum_{n=1}^{n=\infty} b_n \sin(n\theta) = 2 \left[ \frac{2\alpha_p}{(1-2\alpha_p)} \sum_{n=1}^{n=\infty} \left( \frac{1}{2n\pi\alpha_p} \right)^2 \sin(2n\pi\alpha_p) \sin(n\theta) \right]$$

The first figure shows the bipolar sawtooth wave (labelled as “Waveform”) overlaid with three other waveforms: that associated with just the fundamental (“ $n = 1$ ”), then the waveform associated with fundamental + 2<sup>nd</sup> harmonic (“ $n = 1:2$ ”), then the waveform associated with fundamental + 2<sup>nd</sup> + 3<sup>rd</sup> harmonic (“ $n = 1:3$ ”). It can be seen that using just these first three harmonics, that the replication of the sawtooth waveform is not very good, because of the extremely sharp/rapid changes in this waveform at its ends.



The second figure shows the bipolar sawtooth wave (labelled as “Waveform”) overlaid with three other waveforms: that associated with the fundamental through the 5<sup>th</sup> harmonic (“ $n = 1:5$ ”), then the waveform associated with fundamental through the 6<sup>th</sup> harmonic (“ $n = 1:6$ ”), then the waveform associated with fundamental through the 7<sup>th</sup> harmonic (“ $n = 1:7$ ”).