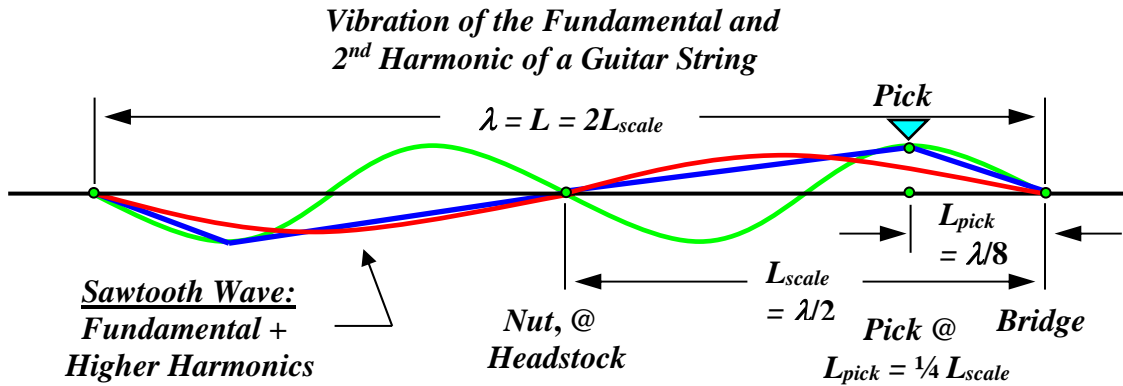


To connect these results with the physical world, we return to the example of the guitar. As shown (again) in the figure below, the scale length, L_{scale} of the guitar corresponds to half the wavelength, λ of the fundamental, for open-string notes played on the guitar, i.e. $L_{scale} = \frac{1}{2} \lambda$. For a pick position distance, L_{pick} (referenced from the bridge of the guitar), this is a fractional distance, $\beta_{pick} \equiv L_{pick} / L_{scale} = 2L_{pick} / \lambda$.



In the following table, we summarize the $\beta_{pick} \equiv L_{pick} / L_{scale}$ locations for the nodes and anti-nodes associated with the first 10 harmonics. Playing at the anti-node locations will result in enhancing that particular harmonic, while playing at the nodal-locations will cause that harmonic to be absent. Physically, values of $\beta_{pick} \equiv L_{pick} / L_{scale} < \frac{1}{2}$ correspond to playing between the bridge and the bottom end of the neck, at the body of the guitar. Smaller values of $\beta_{pick} \equiv L_{pick} / L_{scale}$ are closer to the bridge end of the guitar.

Harmonic # n	$\beta_{pick} \equiv L_{pick} / L_{scale}$ for Node	$\beta_{pick} \equiv L_{pick} / L_{scale}$ for Anti-Node
1 (Fundamental)	–	$\frac{1}{2}$
2	$\frac{1}{2}$	$\frac{1}{4}, \frac{3}{4}$
3	$\frac{1}{3}, \frac{2}{3}$	$\frac{1}{6}, \frac{3}{6}=\frac{1}{2}, \frac{5}{6}$
4	$\frac{1}{4}, \frac{2}{4}=\frac{1}{2}, \frac{3}{4}$	$\frac{1}{8}, \frac{3}{8}, \frac{5}{8}, \frac{7}{8}$
5	$\frac{1}{5}, \frac{2}{5}, \frac{3}{5}, \frac{4}{5}$	$\frac{1}{10}, \frac{3}{10}, \frac{5}{10}=\frac{1}{2}, \frac{7}{10}, \frac{9}{10}$
6	$\frac{1}{6}, \frac{2}{6}=\frac{1}{3}, \frac{3}{6}=\frac{1}{2}, \frac{4}{6}=\frac{2}{3}, \frac{5}{6}$	$\frac{1}{12}, \frac{3}{12}=\frac{1}{4}, \frac{5}{12}, \frac{7}{12} \dots$
7	$\frac{1}{7}, \frac{2}{7}, \frac{3}{7}, \frac{4}{7}, \frac{5}{7}, \frac{6}{7}$	$\frac{1}{14}, \frac{3}{14}, \frac{5}{14}, \frac{7}{14}=\frac{1}{2}, \frac{9}{14} \dots$
8	$\frac{1}{8}, \frac{2}{8}=\frac{1}{4}, \frac{3}{8}, \frac{4}{8}=\frac{1}{2}, \frac{5}{8}, \dots$	$\frac{1}{16}, \frac{3}{16}, \frac{5}{16}, \frac{7}{16}, \frac{9}{16}, \frac{11}{16}, \dots$
9	$\frac{1}{9}, \frac{2}{9}, \frac{3}{9}=\frac{1}{3}, \frac{4}{9}, \frac{5}{9}, \dots$	$\frac{1}{18}, \frac{3}{18}=\frac{1}{6}, \frac{5}{18}, \frac{7}{18}, \dots$
10	$\frac{1}{10}, \frac{2}{10}=\frac{1}{5}, \frac{3}{10}, \frac{4}{10}, \frac{5}{10}, \dots$	$\frac{1}{20}, \frac{3}{20}, \frac{5}{20}=\frac{1}{4}, \frac{7}{20}, \dots$

Thus, from the above table, we can see that for playing on nodes associated with the n^{th} harmonic, that $\beta_{pick} \equiv L_{pick} / L_{scale} = m / n$, where n is the harmonic #, and m is an integer such that $m = 1, 2, 3, \dots < n$. For playing on anti-nodes associated with the n^{th} harmonic, we see that $\beta_{pick} \equiv L_{pick} / L_{scale} = (2m - 1) / 2n$, where again, m is an integer such that $m = 1, 2, 3, \dots < n$.