The total amplitude,  $A_{tot}(t) = A_1(t) + A_2(t)$  vs. time, t is shown in the figure below, for timeindependent/constant frequencies of  $f_1 = 1000$  Hz and  $f_2 = 980$  Hz, equal amplitudes of unit strength,  $A_{10} = A_{20} = 1.0$  and zero relative phase,  $\Delta \phi_{21} = 0.0$ 



Clearly, the beats phenomenon can be seen in the above waveform of total amplitude,  $A_{tot}(t) = A_1(t) + A_2(t)$  vs. time, t. From the above graph, it is obvious that the beat period,  $\tau_{beat} = 1/f_{beat} = 0.050$  sec =  $1/20^{th}$  sec, corresponding to a beat frequency,  $f_{beat} = 1/\tau_{beat} = 20$  Hz, which is simply the frequency difference,  $f_{beat} \equiv |f_1 - f_2|$  between  $f_1 = 1000$  Hz and  $f_2 = 980$  Hz. Thus, the beat period,  $\tau_{beat} = 1/f_{beat} = 1/|f_1 - f_2|$ . When  $f_1 = f_2$ , the beat period becomes infinitely long, and no beats are heard.

2 ©Professor Steven Errede, Department of Physics, University of Illinois at Urbana-Champaign, Illinois 2002-2017. All rights reserved.