

Solution

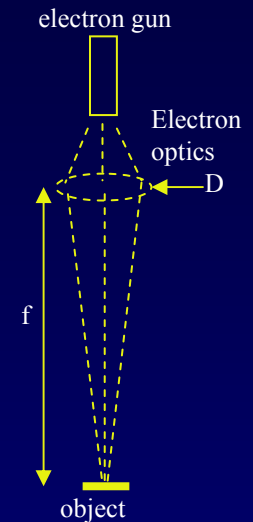
You wish to observe a virus with a diameter of 20 nm, much too small to observe with an optical microscope. Calculate the voltage required to produce an electron wavelength suitable for studying this virus with a resolution of $d_{\min} = 2 \text{ nm}$. The “f-number” for an electron microscope is quite large: $f/D \approx 100$.

Hint: First find λ required to achieve d_{\min} .
Then find E of an electron from λ .

$$d_{\min} \approx 1.22 \frac{\lambda}{D} f$$

$$\lambda \approx d_{\min} \left(\frac{D}{1.22f} \right) = 2 \text{ nm} \left(\frac{D}{1.22f} \right) = 0.0164 \text{ nm}$$

→
$$E = \frac{h^2}{2m\lambda^2} = \frac{1.505 \text{ eV} \cdot \text{nm}^2}{(0.0164 \text{ nm})^2} = 5.6 \text{ keV}$$



Note:

$1.22\lambda/D$ is the diffraction angle, θ
 f is the lever arm,
So, θf is the spot size.

To accelerate an electron to an energy of 5.6 keV requires 5.6 kilovolts .
(The convenience of electron-volt units)