

Solution

There are many times you would like to focus a laser beam to as small a spot as possible. However, diffraction limits this.



The circular aperture of a laser ($\lambda = 780 \text{ nm}$) has $D_{\text{laser}} = 5 \text{ mm}$. What is the spot-size d of the beam after passing through a perfect lens with focal length $f = 5 \text{ mm}$ and diameter $D_{\text{lens}} = 6 \text{ mm}$?

The angular spread of the beam is determined by the smaller of D_{laser} and D_{lens} . Here, it's D_{laser} .

$$\theta_o = 1.22\lambda / D_{\text{laser}}$$

Light at this angle will intercept the focal plane at $d/2 \sim f \theta_o$.

$$\begin{aligned} d &\approx 2\theta_o f = 2.44\lambda f / D_{\text{laser}} \\ &= 2.44(0.78\mu\text{m})(5\text{mm}) / (5\text{mm}) = \boxed{1.9\mu\text{m}} \end{aligned}$$