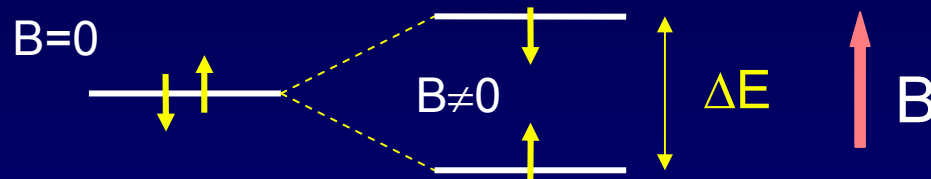


Solution

Magnetic resonance imaging (MRI) depends on the absorption of electromagnetic radiation by the nuclear spin of the hydrogen atoms in our bodies. The nucleus is a proton with spin $\frac{1}{2}$, so in a magnetic field B there are two energy states. The proton's magnetic moment is $\mu_p = 1.41 \times 10^{-26} \text{ J/Tesla}$.



1) The person to be scanned by an MRI machine is placed in a strong (1 Tesla) magnetic field. What is the energy difference between spin-up and spin-down proton states in this field?

$$\begin{aligned}\Delta E &= 2\mu_p B \\ &= 2 \cdot (1.41 \times 10^{-26} \text{ J/T}) \cdot (1 \text{ T}) \\ &= 2.82 \times 10^{-26} \text{ J} = 1.76 \times 10^{-7} \text{ eV}\end{aligned}$$

2) What photon frequency, f , will be absorbed?

$$\begin{aligned}f &= E/h \\ &= (2.82 \times 10^{-26} \text{ J}) / (6.63 \times 10^{-34} \text{ J}\cdot\text{s}) \\ &= 4.26 \times 10^7 \text{ Hz}\end{aligned}$$

