## Tunneling Through a Barrier (1)

What is the the probability that an incident particle tunnels through the barrier? It's called the "Transmission Coefficient, T". Consider a barrier (II) of height  $U_0$ . U = 0 everywhere else.



Getting an exact result requires applying the boundary conditions at x = 0 and x = L, then solving six transcendental equations for six unknowns:

 $\psi_{I}(x) = A_{1} \sin kx + A_{2} \cos kx$  $\psi_{II}(x) = B_{1}e^{Kx} + B_{2}e^{-Kx}$  $\psi_{III}(x) = C_{1} \sin kx + C_{2} \cos kx$ 

 $A_1$ ,  $A_2$ ,  $B_1$ ,  $B_2$ ,  $C_1$ , and  $C_2$  are unknown. K and k are known functions of E. This is more complicated than the infinitely wide barrier, because we can't require that  $B_1 = 0$ . (Why not?)