

Solution

3. Compare the energy $E_{1,\text{finite}}$ of the lowest state of a finite well with the energy $E_{1,\text{infinite}}$ of the lowest state of an infinite well of the same width L .

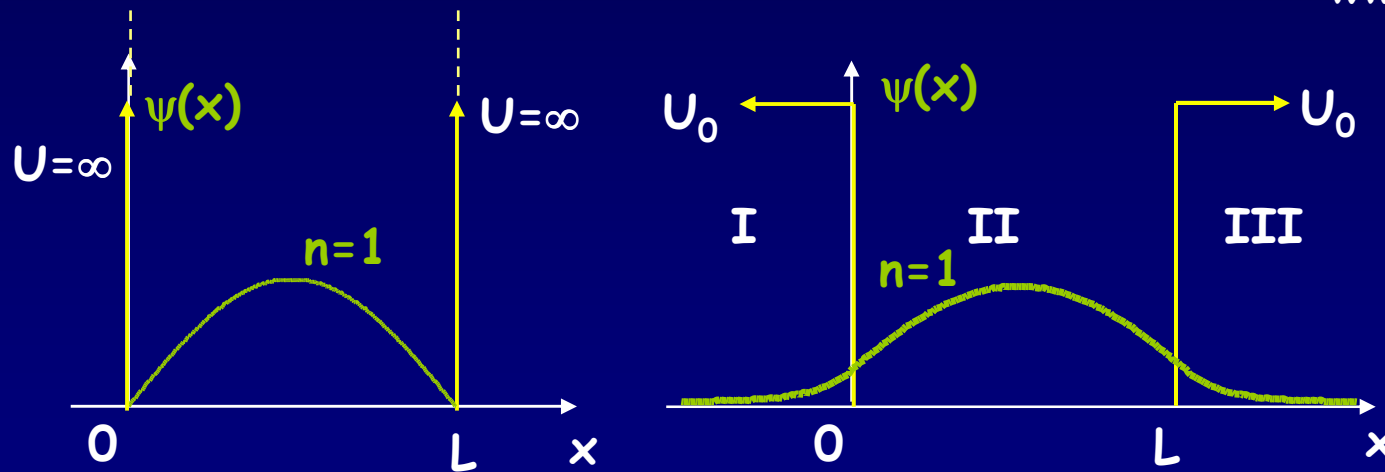
a. $E_{1,\text{finite}} < E_{1,\text{infinite}}$

b. $E_{1,\text{finite}} > E_{1,\text{infinite}}$

c. $E_{1,\text{finite}} = E_{1,\text{infinite}}$

Look at the wavefunctions for the two situations:

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The wavelength in the finite well is longer, because it is not required to go to zero at $x = 0$ and $x = L$ (it “leaks” out a little). Thus, the momentum $p = h/\lambda$ is smaller, and so is the energy. That’s true in general; the less one confines an object, the lower its energy can be - a consequence of the Heisenberg Uncertainty Principle.

Kruse Demo
(wvfn)