

# Particle in a Box (4)

Now, match  $\psi$  at the right boundary ( $x = L$ ).

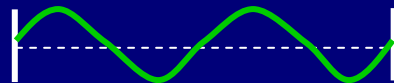
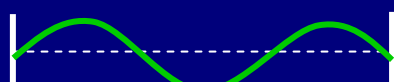
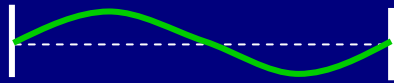

At  $x = L$ :  $\psi_I(L) = \psi_{II}(L)$

$\Rightarrow 0 = B_1 \sin(kL)$

This constraint requires  $k$  to have special values:

$k_n = \frac{n\pi}{L}$   $n = 1, 2, \dots$  Using  $k = \frac{2\pi}{\lambda}$ , we find:  $n\lambda = 2L$

This is the same condition we found for confined waves, e.g., waves on a string, EM waves in a laser cavity, etc.:

	$n$	$\lambda (= v/f)$
	4	$L/2$
	3	$2L/3$
	2	$L$
	1	$2L$

For matter waves, the wavelength is related to the particle energy:

$E = h^2/2m\lambda^2$

Therefore 

