Big Idea

Last time we defined the electric potential energy of charge q in an electric field:

$$\Delta U_{a \to b} = -\int_{a}^{b} \vec{F} \cdot d\vec{l} = -\int_{a}^{b} q \vec{E} \cdot d\vec{l}$$

The only mention of the particle was through its charge q.

We can obtain a new quantity, the electric potential, which is a PROPERTY OF THE SPACE, as the potential energy per unit charge.

$$\Delta V_{a \to b} \equiv \frac{\Delta U_{a \to b}}{q} = -\int_{a}^{b} \vec{E} \cdot d\vec{l}$$

Note the similarity to the definition of another quantity which is also a PROPERTY OF THE SPACE, the electric field. $\vec{E} \equiv \frac{\vec{F}}{}$