

# Checkpoint 2

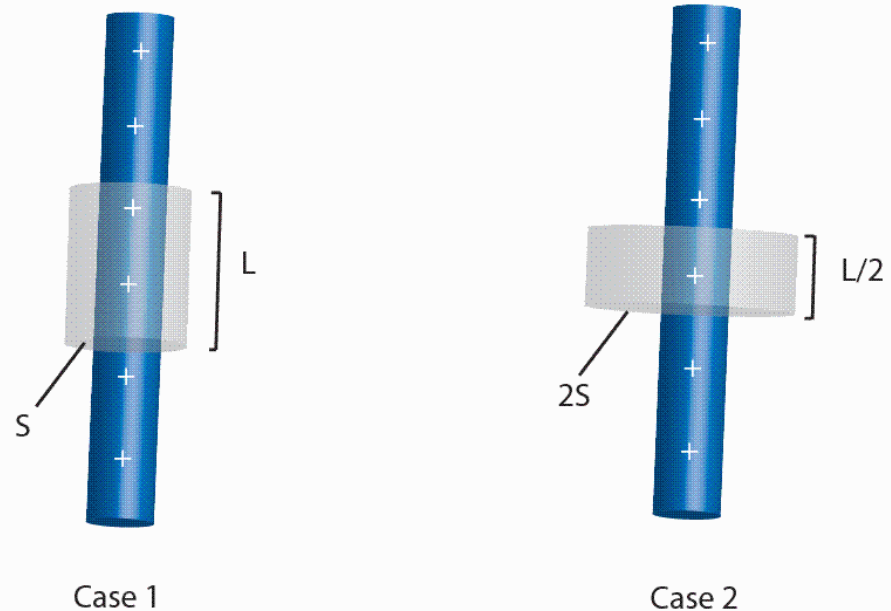
2) An infinitely long charged rod has uniform charge density of  $\lambda$ , and passes through a cylinder (gray). The cylinder in case 2 has twice the cross sectional area and half the length compared to the cylinder in case 1.

## Definition of Flux:

$$\Phi \equiv \int_{\text{surface}} \vec{E} \cdot d\vec{A}$$

$E$  constant on barrel of cylinder  
 $E$  perpendicular to barrel surface  
 ( $E$  parallel to  $dA$ )

$$\begin{aligned} \Phi &= E \int_{\text{barrel}} d\vec{A} \\ &= EA_{\text{barrel}} \end{aligned}$$



$\Phi_1 = 2\Phi_2$ (A)	$\Phi_1 = \Phi_2$ (B)	$\Phi_1 = 1/2\Phi_2$ (C)	none (D)
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Case 1

$$\begin{aligned} A_{\text{barrel}} &= 2\pi sL \\ E_1 &= \frac{\lambda}{2\pi\epsilon_0 s} \end{aligned} \rightarrow \boxed{\Phi_1 = \frac{\lambda L}{\epsilon_0}}$$

Case 2

$$\begin{aligned} A_2 &= (2\pi(2s))L/2 = 2\pi sL \\ E_2 &= \frac{\lambda}{2\pi\epsilon_0(2s)} \end{aligned} \rightarrow \boxed{\Phi_2 = \frac{\lambda(L/2)}{\epsilon_0}}$$

RESULT: GAUSS' LAW

$\Phi$  proportional to charge enclosed !