Time Dilation vs. Length Contraction

• Time intervals between same two events:

Consider only those intervals which occur at one point in rest frame "on train".

- $-\Delta t_0$ is in the reference frame at rest, "on train". "proper time"
- $-\Delta t$ is measured between same two events in reference frame in which train is moving, using clock that isn't moving, "on ground", in that frame.

$$\Delta t_0 = \Delta t \sqrt{1 - \frac{v^2}{c^2}}$$

$$\Delta t > \Delta t_0$$
 Time seems longer from "outside"

• Length intervals of same object:

- $-L_0$ is in reference frame where object is at rest "proper length"
- L is length of moving object measured using ruler that is not moving.

$$L = L_0 \sqrt{1 - \frac{v^2}{c^2}}$$
 Length seems shorter from "outside"