Here are some observations about inverses:

- If A is non-singular (full set of pivots in G-J), then  $A^{-1}$  exists.
- If A has an inverse, then Ax = b has a unique solution:

$$Ax = b \iff A^{-1}Ax = A^{-1}b \iff lx = A^{-1}b \iff x = A^{-1}b$$

• If Ax = 0 has a non-trivial solution (non-trivial null space), then A is not invertible (why?)