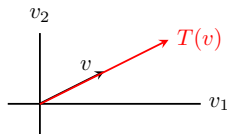


Examples in 2D

Transformations from the plane to the plane ($V = \mathbb{R}^2$, $W = \mathbb{R}^2$) are the easiest to visualize, so let's start there with examples.

Ex A:

$$T(v) = T\left(\begin{bmatrix} v_1 \\ v_2 \end{bmatrix}\right) = \begin{bmatrix} 2v_1 \\ 2v_2 \end{bmatrix} = 2v$$



This transformation is just a **stretch**. Is it linear? Yes:

$$T(c_1u + c_2v) = 2(c_1u + c_2v) = c_1(2u) + c_2(2v) = c_1T(u) + c_2T(v)$$

Ex B:

$$T(v) = T\left(\begin{bmatrix} v_1 \\ v_2 \end{bmatrix}\right) = \begin{bmatrix} -v_2 \\ v_1 \end{bmatrix}$$

