

## Example

- Roll a fair six-sided die, let  $X$  be the value.
- Define

$$A = \{X = 6\}, \quad B = \{X \text{ is even}\}.$$

- Note that  $A \cap B = A$ , since  $A \subseteq B$ . And  $\mathbb{P}(A \cap B) = \mathbb{P}(A) = 1/6$ .
- Then:

$$\mathbb{P}(A|B) = \frac{\mathbb{P}(A \cap B)}{\mathbb{P}(B)} = \frac{1/6}{1/2} = \frac{1}{3},$$

$$\mathbb{P}(B|A) = \frac{\mathbb{P}(A \cap B)}{\mathbb{P}(A)} = \frac{1/6}{1/6} = 1.$$

## Note!!!!!!!!!!!!!!one

- Note that  $P(A|B) \neq P(B|A)$
- Note also that if  $A \subseteq B$  then  $\mathbb{P}(B|A) = 1$ .