• Ok, we have

$$\mathbb{P}(F=n)=\frac{1}{2^n}, n\geq 1.$$

• Is this a probability distribution?

• Yes!

$$\sum_{n=1}^{\infty} \mathbb{P}(F=n) = \sum_{n=1}^{\infty} \frac{1}{2^n} = \frac{1/2}{1-1/2} = 1.$$

• Probability of an even number of flips?

$$\mathbb{P}(\{2,4,6,8,10,\dots\}) = \sum_{\substack{n=1\\n \text{ even}}}^{\infty} \frac{1}{2^n}$$
$$= \sum_{k=1}^{\infty} \frac{1}{2^{2k}} = \sum_{k=1}^{\infty} \frac{1}{4^k} = \frac{1/4}{1-1/4} = \frac{1}{3}.$$