## Discrete Probability Spaces

- Let  $\Omega$  be a countable set (for us usually finite, but not always)
- Assume that we have a function  $p \colon \Omega \to \mathbb{R}$  with the properties:
  - for all  $\omega \in \Omega$ ,  $0 \le p(\omega) \le 1$ ;

$$\sum_{\omega\in\Omega}p(\omega)=1.$$

## Notation

- Ω outcome space or sample space
- each  $\omega \in \Omega$  is an **outcome** or **sample**
- $\Omega$  with the function p is called a **discrete probability space** 
  - "discrete" because Ω is *countable*
- Any subset E ⊆ Ω is called an event.
- We define the probability of the event E as

$$\mathbb{P}(E) := \sum_{\omega \in E} p(\omega).$$