What can go wrong?

- Let X be a set on which we can define addition, i.e. for any $x,y\in X$, $x+y\in X$ is defined.
- Let $A, B \subseteq X$. Then we define

$$A+B=\{a+b:a\in A,b\in B\}.$$

- Now assume that we have some partition of X given by $(A_n)_{n\in I}$.
- Question: is it always true that $A_1 + A_2$ is some A_i ??