

## Definition

We define  $P \iff Q$  to be the proposition that is true when  $P$  and  $Q$  are the same, namely:

$P$	$Q$	$P \iff Q$
T	T	T
T	F	F
F	T	F
F	F	T

We typically read this as “ $P$  if and only if  $Q$ ”, but can also read it as

- “ $P$  iff  $Q$ ”;
- “ $P$  is necessary and sufficient for  $Q$ ”;
- “ $P$  and  $Q$  are (logically) equivalent”.

Note:  $(P \iff Q)$  is **logically** equivalent to:

- 1  $\neg(P \oplus Q)$ ;
- 2  $(P \implies Q) \wedge (Q \implies P)$ .