

## Theorem

Let  $A, B$  be finite sets. Then the following are all equivalent (TFAE):

- 1  $|A| \leq |B|$ ;
- 2 there is an  $f: A \rightarrow B$  injective;
- 3 there is a  $g: B \rightarrow A$  surjective.

TFAE means all are true or all are false — i.e. if we know the truth value of any of these, we know it for all!

Also, this theorem can be stated as saying:

- “Injective means domain is smaller than (or equal to) the codomain”
- “Surjective means domain is larger than (or equal to) the codomain”

However!!<sup>1,000,000,000</sup>

We have assumed that  $A, B$  are finite. This is crucial.