What is a proof?

A (mathematical) proof is an argument designed to convince someone else that a certain mathematical statement is true.