

Or approximate $y(1)$ using $h = .2 = \frac{1}{5}$

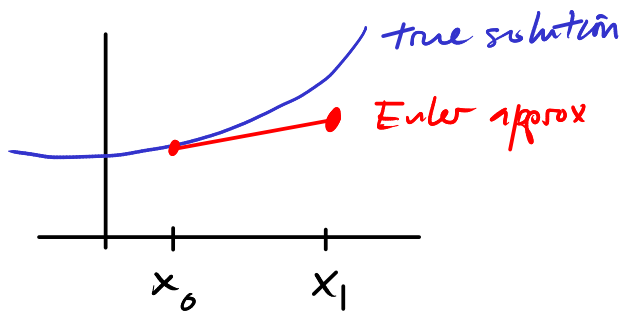
n	0	1	2	3	4	5	
x_n	0	.2	.4	.6	.8	1.0	
y_n	1	1.2	1.48	1.856	2.347	2.976	$y(1) \approx 2.976$
$h \cdot f(x_n, y_n)$.2	.28	.376	.491	.629		

~
rounding
here

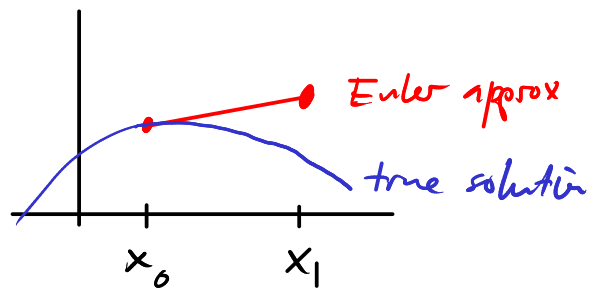
[vs. $y(1) \approx 3$
from before]

different step sizes will give different answers.
Smaller step size and more steps leads to better approximations.
[Though, extremely small step size leads to challenges with representing high precision arithmetic on the computer.]

Error analysis: Like any approximate method, Euler's method introduces errors.



True solution concave up
 \Rightarrow Euler approximation
is an underestimate



True solution concave down
 \Rightarrow Euler approximation is
an over estimate.

More sophisticated numerical methods exist (e.g. Runge-Kutta) that do better with this.