

$$= -\frac{1}{n\pi} (\cos n\pi + \cos n\pi) + 0 - 0$$

$$= -\frac{2}{n\pi} \cos n\pi = \begin{cases} \frac{2}{n\pi} & n \text{ odd} \\ -\frac{2}{n\pi} & n \text{ even} \end{cases}$$

We can also write $\cos n\pi = (-1)^n$

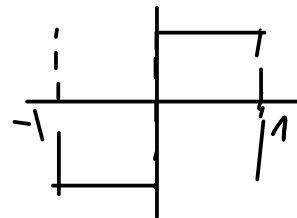
$$\text{So } b_n = -\frac{2}{n\pi} (-1)^n = \frac{2}{n\pi} (-1)^{n+1}$$

So the Fourier series for the sawtooth is

$$f(t) = \sum_{n=1}^{\infty} \frac{2}{n\pi} (-1)^{n+1} \sin n\pi t$$

Compare with square wave of same period

$$\sum_{n \text{ odd}} \frac{4}{n\pi} \sin n\pi t$$



In the square wave, only odd multiples of the fundamental occur.
 In the sawtooth, all multiples of the fundamental occur.
 In both, the amplitude of the n th multiple is proportional to $1/n$.

For triangle wave



Odd multiples of fundamental are present, but the n th has amplitude proportional to $1/n^2$.