

General solution to $m x'' + kx = F_0 \cos \omega t$ ($\omega \neq \omega_0$) is

$$x(t) = c_1 \sin \omega_0 t + c_2 \cos \omega_0 t + \frac{F_0/m}{\omega_0^2 - \omega^2} \cos \omega t$$

$$\text{or } x(t) = C \cos(\omega_0 t - \alpha) + \frac{F_0/m}{\omega_0^2 - \omega^2} \cos \omega t$$

Thus the solution will be a combination of sinusoids at different frequencies. This leads to the phenomenon of beats.