

To be more specific

$t$  = time in seconds

$T$  = temp in Kelvin

$$k = 5 \text{ s}^{-1}$$

$$A = 300 \text{ K}$$

$$T_0 = 2000 \text{ K}$$

$$\begin{aligned} T(t) &= (T_0 - A) e^{-kt} + A \\ &= 1700 e^{-5t} + 300 \end{aligned}$$

Many models involve differential equations

\* Logistic model for population:  $\frac{dP}{dt} = kP(C-P)$   $P(t)$  = pop.

\* Harmonic oscillator:

Mass on spring



$$m \frac{d^2x}{dt^2} + kx = 0$$

$x(t)$  = position

pendulum  
(approximately)



with friction:

$$m \frac{d^2x}{dt^2} + \gamma \frac{dx}{dt} + kx = 0$$

\* Airy equation:  $\frac{d^2y}{dx^2} = xy$  models intensity of the rainbow  
explains (at least approximately)  
the "double rainbow" phenomenon

What differential equation does it solve?

$$y = e^t, \quad \frac{dy}{dt} = y$$

$$y = \frac{1}{1-x}, \quad \frac{dy}{dx} = y^2$$

$$y = \sin t, \quad \frac{d^2y}{dt^2} = -y$$

$$y = \frac{1}{(1-x)^2}, \quad \frac{dy}{dx} = 2y^{3/2}$$