

Newton says

$$\frac{dT}{dt} = -k(T-A)$$

k = constant measuring rate at which heat is conducted to/from the object. Depends on physical composition of the object. k is always positive

This is a differential equation because it involves the derivative $\frac{dT}{dt}$.

We want to know more explicitly what T is as a function of t . In fact

$$T(t) = C e^{-kt} + A$$

Solves the Differential equation, where C is any number.

It's easy to check: Let $T(t) = C e^{-kt} + A$

$$\text{LHS} = \frac{dT}{dt} = \frac{d}{dt}(C e^{-kt}) + \frac{d}{dt}(A) = C \frac{d}{dt}(e^{-kt}) + 0$$

$$= C(-k) e^{-kt} \quad \leftarrow \text{equal!}$$

$$\text{RHS} = -k(T-A) = -k(C e^{-kt} + A - A) = -k C e^{-kt}$$