

When we take the limit of such Riemann Sums, we get

$$\int_a^b f(x) dx = A_2 - A_1$$

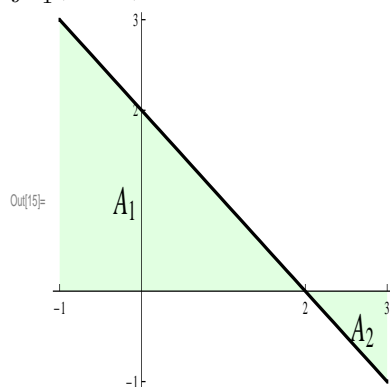
where  $A_2$  is the area of the region above the x-axis and below the graph of  $f$  and  $A_1$  is the area of the region below the x-axis and above the graph of  $f$ .

Side Note If we are interested in the *total area* we need to calculate

$$\int_{-1}^3 |2 - x| dx$$

**Example** Evaluate the integral by interpreting each in terms of area

$$\int_{-1}^3 (2 - x) dx$$



Above we have the graph of the area we are calculating. By discussion preceding this example we know

$$\int_{-1}^3 (2 - x) dx = A_1 - A_2 = \frac{3 \cdot 3}{2} - \frac{1 \cdot 1}{2} = \frac{8}{2} = 4$$