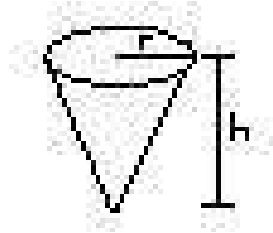


**Example** Consider a conical tank. Its radius at the top is 4 feet, and its 10 feet high. Its being filled with water at the rate of 2 cubic feet per minute. How fast is the water level rising when it is 5 feet high? Here is a rough sketch of the tank



First note that we are given  $r_{top} = 4$  and  $h_{full} = 10$ . Also  $\frac{dV}{dt} = 2ft^3/min$ . We are asked to find the rate of change in the height of the water so we want to find  $\frac{dh}{dt}$  when  $h = 5$ . Since we are given the derivative of the water's volume it is a good idea to use the Conics Volume =  $\frac{1}{3}\pi r^2 h$  formula as the "connection" equation. One problem with it is that we have two variables  $r$  and  $h$  that are changing with time on the right hand side of the equation. So if we take the derivative we will have both  $\frac{dh}{dt}$  and  $\frac{dr}{dt}$  popping up and they are both unknown. We need to figure out either how to find  $\frac{dr}{dt}$  or write  $r$  in terms of  $h$  before doing the differentiation so we have only one variable to deal with. I'll go with writing  $r$  as a function of  $h$  as the other option will require me to do this anyways. To achieve this we need to draw the two-dimensional cross-section of this tank. We will use the letters  $r$  and  $h$  to represent the variable radius and height of the water at any level. We can find the relationship between  $r$  and  $h$  from figure below using similar triangles