

$$F'(x) = \frac{2(x-1)(x+1)-(x-1)^2}{(x+1)^2} = \frac{(x-1)(x+3)}{(x+1)^2}$$

$$F'(x) = 0 \Rightarrow (x-1)(x+3) = 0 \Rightarrow x = 1 \text{ and } x = -3$$

Also the derivative confirms our previous observation $F'(-1)$ is not defined. So the critical values are $x = -3, -1, 1$. To classify these points and where the function is decreasing (\searrow) or increasing (\nearrow) I'll use a similar chart like the one in the previous example. The only difference between this sign chart's construction and the previous one is: I have double-vertical lines emanating from the critical value $x = -1$. This is to distinguish this critical value from the other two (-3 and 1), because this one makes my derivative not defined and other two make it equal to zero.

x	-3	-1	1
F'	$+$	$-$	$+$
F	\nearrow	\searrow	\nearrow

So according to sign chart: F is \nearrow on the intervals $(-\infty, -3)$ and $(1, \infty)$. F is \searrow on the intervals $(-3, -1)$ and $(-1, 1)$. By using the First Derivative Test at $x = -3$ we have a local maximum and at $x = 1$ we have a local minimum

Here we have a rough sketch of F based on the information above.

