

Example Let $y = \frac{3x^2 + 2\sqrt{x}}{x}$ find y'

$$\begin{aligned} f(x) &= 3x^2 + 2\sqrt{x} \Rightarrow f'(x) = 6x + \frac{2}{\sqrt{x}} \\ g(x) &= x \Rightarrow g'(x) = 1 \end{aligned}$$

$$y' = \frac{f'(x)g(x) - g'(x)f(x)}{[g(x)]^2} = \frac{(6x + \frac{2}{\sqrt{x}})x - 1 \cdot (3x^2 + 2\sqrt{x})}{x^2} = \frac{3x^2 - \sqrt{x}}{x^2} = 3 - x^{-3/2}$$

Remark: Again if you don't have to use the Quotient Rule DON'T!!
So in the example above re-write y as $y = 3x + 2x^{-1/2} \Rightarrow y' = 3 - x^{-3/2}$

Example Let $y = \frac{\frac{1}{x}}{x^2 + 1}$ find y'

$$y' = \frac{\frac{-1}{x^2}(x^2 + 1) - \frac{1}{x}(2x)}{(x^2 + 1)^2} = \frac{-3x^2 - 1}{x^2(x^2 + 1)^2}$$