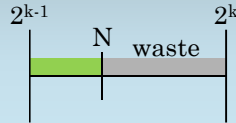


Integrate to Find Expected Waste

The assumption of uniformity gives us a factor of $(2^{k-1})^{-1}$.

Integrating over the interval shown gives us



$$\text{Expected waste} = \frac{1}{2^{k-1}} \int_{2^{k-1}}^{2^k} \left(\frac{2^k}{N} - 1\right) dN$$

The -1 averages to -1 , of course.

The first term averages to $2 \ln 2$.

Dynamic Resizing Adds ~38% Extra Space on Average

Putting those two terms together gives

$$\text{Expected waste} = 2 (\ln 2 - \frac{1}{2})$$

which is **about 38%**.

(Probably not too important.)

We Need Dynamic Allocation for Dynamic Resizing

One last thing before we can write the code:

- the standard **C** library
- dynamic allocation functions
- (`#include <stdlib.h>` for these).

`malloc` Allocates a New Chunk of Memory

The most basic call is

```
void* malloc (size_t size);
```

`size` is the **number of bytes needed**.

`malloc` returns

- **a pointer to a new chunk of memory** (from the heap), or
- **NULL on failure** (memory not available).