University of Illinois at Urbana-Champaign Dept. of Electrical and Computer Engineering

ECE 220: Computer Systems & Programming

More Recursion Examples

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# Ready to Play a Game?

Let's play Nim!

In Nim, there are three piles of sticks...



On their turn, each player

- $\circ\, takes$  as many sticks as they want
- from one of the piles.

The last player to take sticks wins.

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### Is Nim a Forced Win or a Forced Loss

Nim starts with 3, 5, and 7 sticks in the piles.

There is no way to tie.

A forced win means that,

- $\circ\operatorname{if}$  a player plays correctly,
- they are **guaranteed to win**.

#### Is Nim

- a forced win (for the first player),
- or a forced loss?

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## Let's Use Recursion to Evaluate Nim

There's a fairly easy and intuitive mathematical solution to Nim.

But ... maybe you don't know it?

Fortunately, now you know recursion.

#### So let's

- write a recursive function
- to answer the question!

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